



THE VILLAGE
INTERNATIONAL SCHOOL
"We Nurture Dreams"

DEPARTMENT OF MATHEMATICS

CLASS12

CHAPTER1- RELATIONS &FUNCTIONS

- 1) Let R be a relation on the set L of lines defined by $l_1 R l_2$ if l_1 is perpendicular to l_2 , then relation R is
 - (a) reflexive and symmetric
 - (b) symmetric and transitive
 - (c) equivalence relation
 - (d) symmetric
- 2) 2. Given triangles with sides $T_1 : 3, 4, 5$; $T_2 : 5, 12, 13$; $T_3 : 6, 8, 10$; $T_4 : 4, 7, 9$ and a relation R in set of triangles defined as $R = \{(\Delta_1, \Delta_2) : \Delta_1 \text{ is similar to } \Delta_2\}$. Which triangles belong to the same equivalence class?
 - (a) T_1 and T_2
 - (b) T_2 and T_3
 - (c) T_1 and T_3
 - (d) T_1 and T_4
- 3) 3. Given set $A = \{1, 2, 3\}$ and a relation $R = \{(1, 2), (2, 1)\}$, the relation R will be
 - (a) reflexive if $(1, 1)$ is added
 - (b) symmetric if $(2, 3)$ is added
 - (c) transitive if $(1, 1)$ is added
 - (d) symmetric if $(3, 2)$ is added
- 4) 4. Given set $A = \{a, b, c\}$. An identity relation in set A is
 - (a) $R = \{(a, b), (a, c)\}$
 - (b) $R = \{(a, a), (b, b), (c, c)\}$
 - (c) $R = \{(a, a), (b, b), (c, c), (a, c)\}$
 - (d) $R = \{(c, a), (b, a), (a, a)\}$
- 5) . A relation S in the set of real numbers is defined as $xSy \Rightarrow x - y + \sqrt{3}$ is an irrational number, then relation S is
 - (a) reflexive
 - (b) reflexive and symmetric
 - (c) transitive
 - (d) symmetric and transitive
- 6) 6. Set A has 3 elements and the set B has 4 elements. Then the number of injective functions that can be defined from set A to set B is
 - (a) 144

- (b) 12
 (c) 24
 (d) 64
- 7) Let Z be the set of integers and R be a relation defined in Z such that aRb if $(a - b)$ is divisible by 5. Then R partitions the set Z into _____ pairwise disjoint subsets.
- 8) Consider set $A = \{1, 2, 3\}$ and the relation $R = \{(1, 2)\}$, then? is a transitive relation. State true or false.
- 9) Every relation which is symmetric and transitive is reflexive also. State true or false.
- 10) Let R be a relation defined as $R = \{(x, x), (y, y), (z, z), (x, z)\}$ in set $A = \{x, y, z\}$ then R is (reflexive/symmetric) relation.
- 11) Let R be a relation in the set of natural numbers N defined by $R = \{(a, b) \in N \times N : a < b\}$. Is relation R reflexive? Give a reason.
- 12) Let A be any non-empty set and $P(A)$ be the power set of A . A relation R defined on $P(A)$ by $X R Y \Leftrightarrow X \cap Y = X, X, Y \in P(A)$. Examine whether? is symmetric.
- 13) State the reason for the relation R in the set $\{1, 2, 3\}$ given by $R = \{(1, 2), (2, 1)\}$ not to be transitive.
- 14) State the reason for the relation R in the set $\{1, 2, 3\}$ given by $R = \{(1, 2), (2, 1)\}$ not to be transitive.
- 15) Show that the relation R in the set $\{1, 2, 3\}$ given by $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 3)\}$ is reflexive but neither symmetric nor transitive.
- 16) Let $A = \{3, 4, 5\}$ and relation R on set A is defined as $R = \{(a, b) \in A \times A : a - b = 10\}$. Is relation an empty relation?
- 17) Given set $A = \{a, b\}$ and relation R on A is defined as $R = \{(a, a), (b, b)\}$. Is relation an identity relation?
- 18) 19. Let set A represents the set of all the girls of a particular class. Relation R on A is defined as $R = \{(a, b) \in A \times A : \text{difference between weights of } a \text{ and } b \text{ is less than } 30 \text{ kg}\}$. Show that relation R is a universal relation.
- 19) If $A = \{1, 2, 3\}$ and relation $R = \{(2, 3)\}$ in A . Check whether relation R is reflexive, symmetric and transitive.
- 20) State the reason for the relation R in the set $\{1, 2, 3\}$ given by $R = \{(1, 2), (2, 1)\}$ not to be transitive.
- 21) Consider the set A containing n elements, then the total number of injective functions from set A onto itself is _____ .
- 22) The domain of the function $f : R \rightarrow R$ defined by $f(x) = \sqrt{4 - x^2}$ is _____
- 23) Let $A = \{a, b\}$. Then number of one-one functions from A to A possible are

- (a) 2
 (b) 4
 (c) 1
 (d) 3
- 24) Let $A = \{1, 2, 3, 4\}$ and $B = \{a, b, c\}$. Then number of one-one functions from A to B are _____.
- 25) If $n(A) = p$, then number of bijective functions from set A to A are _____ ..
- 26) The function $f: \mathbb{R} \rightarrow \mathbb{R}$ defined as $f(x) = [x]$, where $[x]$ is greatest integer $\leq x$, is onto function. State true or false.
- 27) Let $A = \{1, 2, 3\}$, $B = \{4, 5, 6, 7\}$ and let $f = \{(1, 4), (2, 5), (3, 6)\}$ be a function from A to B. State whether f is one-one or not
- 28) Let $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by $f(x) = |x|$. Is function f onto? Give a reason.
- 29) Prove that $f: \mathbb{R} \rightarrow \mathbb{R}$ given by $f(x) = x^3 + 1$ is one-one function.
- 30) Show that the Signum Function $f: \mathbb{R} \rightarrow \mathbb{R}$,

$$\text{given by } f(x) = \begin{cases} 1, & \text{if } x > 0 \\ 0, & \text{if } x = 0 \\ -1, & \text{if } x < 0 \end{cases} \text{ is neither}$$

one-one nor onto.

- 31) Given $f(x) = \sin x$ check if function f is one-one for (i) $(0, \pi)$
 (ii) $(-\pi/2, \pi/2)$.

ANSWERS

<https://www.ncertbooks.guru/maths-mcqs-for-class-12-with-answers-chapter-1/>

4 MARK QUESTIONS

- 1) Consider $f: \mathbb{R} \rightarrow \mathbb{R}$ given by $f(x) = 9x^2 + 6x - 5$. Show that f is one to one but not onto.
- 2) Let $f: \mathbb{N} \rightarrow \mathbb{R}$ be a function defined as $f(x) = 4x^2 + 12x + 15$. show that f is one to one but not onto.
- 3) Let $A = \{1, 2, 3, \dots, 10\}$ and R be the relation in $A \times A$ defined by $(a, b) R (c, d)$ iff $a + d = b + c$ for $(a, b), (c, d)$ in $A \times A$. Prove that R is an equivalence relation. Also obtain the equivalence class $[(3, 4)]$.
- 4) Let $A = \{1, 2, 3, \dots, 9\}$ and R be the relation in $A \times A$ defined by $(a, b) R (c, d)$ if $a + d = b + c$ for $(a, b), (c, d)$ in $A \times A$. Prove that R is an equivalence relation. Also obtain the equivalence class $[(2, 5)]$.

5)

Let N denote the set of all natural numbers and R be the relation on $N \times N$ defined by $(a, b) R (c, d)$ iff $ad(b+c) = bc(a+d)$. Show that R is an equivalence relation.

- 6) Show that the relation R in the set N of Natural numbers given by $R = \{(a, b) : 3 \text{ divides } |a - b|\}$ is not an equivalence relation.
- 7) Check whether the relation R in \mathbf{R} defined by $R = \{(a, b) : a \leq b^3\}$ is reflexive, symmetric, transitive.
- 8) Prove the relation R on the set $N \times N$ defined by $(a, b) R (c, d) \Leftrightarrow ad=bc$ for all $(a, b), (c, d) \in N \times N$ is an equivalence relation.