



CLASS12

THE VILLAGE
INTERNATIONAL SCHOOL
"We Nurture Dreams"

Max.Marks: 20

05-11-24

MATHEMATICS(041) – MT3

Time: 50 minutes

General Instructions:

- 1) Questions 1 to 4 carries 1 mark each.
- 2) Questions 5 to 8 carries 2 marks each.
- 3) Questions 9 and 10 carries 4 marks each.

| SECTION A | | |
|-----------|---|---|
| 1. | Evaluate: $\int \frac{\sin^2 x - \cos^2 x}{\sin^2 x \cos^2 x} dx$ (a) $\tan x - \cot x + C$ (c) $\tan x + \cot x + C$ | 1 (b) $-\tan x + \cot x + C$ (d) $-\tan x - \cot x + C$ |
| 2. | The value of $\int_0^a \frac{\sqrt{x}}{\sqrt{x} + \sqrt{a-x}} dx$ is: (a) $a/2$ | 1 (b) a (c) a^2 (d) 0 |
| 3. | The value of $\int \frac{e^x}{e^x(e^x+1)} dx$ is: (a) $\log \left \frac{e^x}{e^x+1} \right + C$ (c) $\log \log \frac{1}{e^x} + C$ | 1 (b) $\log 1 - e^{-x} + C$ (d) $\log e^x + 1 + C$ |
| 4. | Evaluate $\int_0^{\frac{\pi}{2}} \frac{\sin^2 x}{\sin^2 x + \cos^2 x} dx$ a) 1 b) 0 c) $\frac{\pi}{2}$ | 1 d) $\frac{\pi}{4}$ |
| SECTION B | | |
| 5. | Evaluate $\int \frac{1}{x^2+49} dx$ | 2 ANS) $1/7 \tan^{-1}\left(\frac{x}{7}\right)$ |
| 6. | Evaluate $\int \cot x \log \sin x dx$ | 2 ANS) $\left(\frac{\log \sin x)^2}{2}\right) + c$ |
| OR | | |

| | | |
|-----------|---|---|
| | Evaluate $\int e^x \sin x \, dx$ | |
| 7. | Evaluate $\int e^x \left(\frac{1}{x} - \frac{1}{x^2} \right) \, dx$ ANS) $e^x/x + c$ | 2 |
| 8. | Evaluate $\int_2^5 x - 4 \, dx$ ANS) $\int_2^4 4 - x + \int_4^5 x - 4 \, dx = 5/2$ | 2 |
| SECTION C | | |
| 9. | Evaluate : $\int (x \tan^{-1} x) \, dx$ ANS) $\frac{x^2}{2} \tan^{-1} x - \frac{x}{2} + \tan^{-1} x + c$ OR Evaluate $\int_1^4 \{ x - 1 + x - 2 + x - 3 \} \, dx$ | 4 |
| 10. | Evaluate: $\int \frac{3x+1}{(x-1)^2(x+3)} \, dx$ ANS) $-1/2 \log(x+3) + 1/2 \log(x-1) - \frac{1}{x-1} + c$ | 4 |